

## PROSIMPLUS APPLICATION EXAMPLE

# EXAMPLE OF USE OF AN EXTERNAL OPTIMIZATION ALGORITHM

**EXAMPLE PURPOSE** 

This example illustrates the use of an external optimization algorithm in the ProSimPlus simulation environment.

The communication interfaces with the external algorithm are detailed along with a short application example.

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CORRESPONDING PROSIMPLUS FILES	PSPS_EX_EN-External-optimizer-example.pmp3
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Energy

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The ProSimPlus simulation environment contains in its standard library two optimization algorithms, the first one is based on a SQP method (Sequential Quadratic Programming) and the second is implementing an evolutionary algorithm (genetic algorithm). Both of them are only working with continuous variables corresponding to the operating parameters of the process to be modeled. With the aim to offer more flexibility to the end-user, a new feature has been developed in version 3.5.16 of ProSimPlus; it allows to use an external optimization algorithm that can handle any type of optimization problem (multi-objective with continuous, integer or logical variables) through an external dynamic library. This document presents an example of use of this feature.

In a first step, the operating mode of the standard ProSimPlus optimizer is reminded, then the second part is dedicated to the presentation of the communication interfaces and finally an example based on the MIDACO optimization algorithm (<u>www.midaco-solver.com</u>) is detailed. MIDACO uses an extended "Ant Colony Optimization" evolutionary algorithm and is able to deal with multi-objective problems with mixed variables.

#### 2. OPERATING MODE OF THE PROSIMPLUS STANDARD OPTIMIZER

#### 2.1. Principle

The main operating principle of the ProSimPlus optimizer rely on a sequence of back to back runs (called « runs in the MCN ») between the module itself and the unit operations belonging to the optimization loop. This operating mode rely on the fact that the optimizer needs to know the values of the objective functions and the constraints at different steps of the optimization process:

- At the start of the convergence process
- When the objective functions and the constraints are being evaluated for a set of iterative variables at the current iteration
- When the derivatives of the objective functions and of the constraints are being calculated through numerical perturbations between two successive iterations

The description of the problem to be solved and the parameters associated to the SQP algorithm are detailed in the user's manual to which one's will refer for any additional information, especially concerning the **Feasible Path** and **Unfeasible Path** approaches as well as for the multi-periods optimization.

Thus, it's the role of the optimization algorithm to deal with the current calculation phase and depending on the type of algorithm used, the number of calculation phases can be variable. An evolutionary algorithm, for example, does only functions evaluations for different populations and after mutation and crossing, restarts the evaluation process until it reaches the predefined maximum number of generations.

#### 2.2. Management of "tear" streams

Without describing in full details the **Unfeasible Path** approach, one's must know that the presence of "tear" streams in the optimization loop impose to the optimizer to handle the variables associated with these "tear" streams as optimization variables and to write equality constraints related to these variables, in form of:

$$x - g(x) = 0$$

With: *x* Current value of the variable

g(x) Value of the variable after a run in the MCN.

The variables associated to a "tear" stream are: the partial molar flowrates of the components involved in the simulation and possibly the temperature and the pressure of the stream. Generally the temperature is taken into account whereas the pressure is added only if the unit operation from which the stream is exiting is automatically adjusting the pressure (for example the "Pipe segment" unit).

Furthermore, the variables associated to the "tear" streams must be the first variables of the optimization variables array (action variables) and in the following order:

Partial molar flowrate of the component #1 in the "tear" stream #1

Partial molar flowrate of the component #2 in the "tear" stream #1

•••

Partial molar flowrate of the component #NC in the "tear" stream #1

Temperature of the "tear" stream #1 (if the temperature is selected as an optimization variable)

Pressure of the "tear" stream #1 (if the pressure is selected as an optimization variable)

. . . .

The other optimization variables (outlet information streams from the "Optimization" unit) come after.

The use of an external optimization algorithm does not deviate from this rule as soon as it's the **Unfeasible Path** approach which is used.

The **Feasible Path** approach, which imposes the use of a "Constraints and recycles" unit, allows to ignore this rule, even if in this case the calculation sequence must then be manually supplied (see ProSimPlus user's manual).

#### 2.3. Management of information

The various information required by the "Optimization" unit, are transmitted thanks to information streams connected to the unit and in the following sequence:

- Inlet information
  - 1. Objective function
  - 2. Equality constraint #1
  - 3. ...
  - 4. Equality constraint #NE
  - 5. Inequality constraint #1
  - 6. ...
  - 7. Inequality constraint #NI
- Outlet information
  - 1. Action variable #1
  - 2. ...
  - 3. Action variable #NA

In the standard version of the optimizer (SQP algorithm), only one objective function is allowed, this means that the multi-objective optimization is not possible. However, an external algorithm might be able to handle several objective functions, thus the possibility to connect several objective functions has been implemented. For the standard SQP algorithm, this limitation is still in use, whereas for an external algorithm up to 10 objective functions (i.e. inlet information streams) can be connected to perform a multi-objective optimization.

#### 2.4. Parameters

In order to offer the best user-friendliness in the use of an external algorithm, most of the standard parameters of the "Optimization" unit have been kept and can be used along with the external algorithm. These parameters are the following ones:

- Selection of the "tear" streams
- Selection of the parameters associated to the « tear » streams: bounds and increments for a possible sensitivity analysis
- Parameters relating to the optimization variables (action variables) : bounds, increments and types of increments for the sensitivity analysis
- General numerical parameters: maximum number of runs in the MCN, maximum number of iterations, intermediate printings step, number of rest steps, number of equality constraints, number of periods

Concerning the external algorithm-specific parameters, they are available in a « spreadsheet » like grid, allowing to adapt to the specificity of each external algorithm by offering the best flexibility of use.

### **3. COMMUNICATION INTERFACES WITH THE EXTERNAL ALGORITHM**

Two communication interfaces are available, respectively for the calculation itself and for the printing of the results. They are detailed hereafter.

#### 3.1. Calling interface for the solving

The calling interface used during the solving, is presented below:

The calling convention used is **STDCALL** and the arguments are passed by reference. The name of the entry point is imposed and must be **OPTI** (in uppercase).

The meaning of the function arguments is given in the following table:

## Example of use of an external optimization algorithm Version : March 2024

Name	Туре	Size (bytes)	I/O	Dimension	Description
NPT	Integer	4	I	1	Number of user parameters
ITEMAX	Integer	4	I	1	Maximum number of iterations
NAPM	Integer	4	I	1	Maximum number of runs in the MCN
IALP	Integer	4	I	NVA	Types of increment of the sensitivity analysis IALP(i)=1 : Absolute, IALP(i)=2 : Proportional
NCO	Integer	4	I	1	Number of constraints
NCI	Integer	4	I	1	Number of inequality constraints
NVA	Integer	4	I	1	Number of optimization variables
NF	Integer	4	I	1	Number of objective functions
ITER	Integer	4	I/O	1	Current iteration count
КОРТ	Integer	4	I/O	1	Index of the calculation phase
INFO	Integer	4	0	1	Information relative to the calculation stop
PAR	Float	8	I/O	NPT	Array of parameters for the external algorithm
F	Float	8	I	NF	Array of the objective functions
С	Float	8	I/O	NCO	Array of the constraints
XL	Float	8	I	NVA	Array of the lower bounds of the action variables
XU	Float	8	I	NVA	Array of the upper bounds of the action variables
AC	Float	8	I	NVA	Array of the increments for the sensitivity analysis
X	Float	8	I/O	NVA	Array of the optimization variables
G	Float	8	I/O	(NF,NVA)	Work array for the storage of the derivatives of the objective functions with respect to the optimization variables
CN	Float	8	I/O	(NCO,NVA)	Work array for the storage of the derivatives of the constraints with respect to the optimization variables

Note: The **G()** and **CN()** arrays are provided as storage arrays for the derivatives of the objective functions and derivatives of the constraints with respect to the optimization variables and may not be used depending on the optimization algorithm used.

At each call, the function must return an integer value indicating the current state of the calculation.

The return code can take the following values:

OPTI_RUNNING	-1	Optimization running
OPTI_CONVERGED	0	Optimization ended
OPTI_FAILED	2	Optimization failed

Furthermore, during the calculation, the **KOPT** variable is used by the **OPTI** function to know and manage the current calculation state. The **KOPT** variable is set to 0 at first call (which allows to perform some initializations or to execute specific code only once) and must be set to any non-zero value by the function. The values are let free to the developer's needs. At the end of the optimization process, the **KOPT** variable must be reset to zero (i.e. when the return code has been set to **OPTI\_CONVERGED** or **OPTI\_FAILED**).

Then, the **INFO** variable is used to know the reason of the calculation stop. This variable can take the following values:

INFO	Description
1	Optimization successful
≠ 1	Failure of the optimization

#### 3.1. Calling interface for the printings

The calling interface used for the printings, is presented below:

```
subroutine IOPTI(PAR,NPT)
!dec$ attributes stdcall, reference, alias:'IOPTI', dllexport :: IOPTI
    integer(4), intent(in) :: NPT
    real(8), intent(in) :: PAR(NPT)
```

The calling convention used is **STDCALL** and the arguments are passed by reference. The name of the entry point is imposed and must be **IOPTI** (in uppercase).

The meaning of the arguments is the same as for the main calling interface (OPTI function above).

**Note**: The entry point is optional, if it is not available in the dynamic link library, it will not be called but this will not prevent the optimization process to run. In the case it is available, the printings must be made into specific file, named **IMPO\_OPTI.tmp** and being located in the temporary folder of the current user. This file must be open in the **IOPTI** subroutine and closed before leaving it in order to the calling process to be able to read its content and to destroy it after. This file can be used, for example, to transfer the contents of the output file(s) generated by the external algorithm to the simulation report. If needed, the external algorithm-specific parameters are available in the arguments list but must not be modified (read only).

#### 3.2. Management of objective functions

The **F()** array contains the value(s) of the objective function(s) for the current optimization process. It contains the values transmitted to the "Optimization" unit through information stream(s) connected to the connection ports labelled "Objective function i". The **F()** array is updated at each call with the current value(s) of the objective function(s). In the case of an optimization algorithm requiring to evaluate the derivatives of the objective function(s) with respect to the optimization variables, it will be necessary to save the contents of this array into a local array at the beginning of every new iteration (i.e. once the evaluation of the objective function(s) and the constraints has been performed).

#### 3.3. Management of constraints

The **G()** array contains the values of the constraints for the current optimization process. It contains the values of the equality constraints followed by those of the inequality constraints. In the case the "Optimization" unit handles by itself the "tear" streams, i.e. in the case of the **Unfeasible Path** approach, the equality constraints are first made up with the constraints relating to the « tear » streams followed by the constraints transmitted to the "Optimization" unit through the information streams connected to the connection ports labelled "Constraint i".

Furthermore, the connection ports, labelled "Constraint 1" to "Constraint NE" must compulsorily be used for the **NE** equality constraints and the ports "Constraint NE+1" to "Constraint NE+NI" by those associated to the inequality constraints.

As for the objective function(s), the **G()** array is updated at each call with the current values of the constraints. In the case of an optimization algorithm requiring to evaluate the derivatives of the constraints with respect to the optimization variables, it will be necessary to save the contents of this array into a local array at the beginning of every new iteration (i.e. once the evaluation of the objective function(s) and the constraints has been performed).

#### 3.3.1. Inequality constraints

The inequality constraints must be written in such a way that the value of the constraint is negative when it is satisfied, which is the normal behavior used in the standard optimization algorithm (SQP). For example, if a constraint is expressed as:

$$a \leq f_i \leq b$$

Then, the G() array will contains the following expressions:

$$G(k) = a - f_i$$
$$G(k + 1) = f_i - b$$

In the case where the external algorithm uses the reverse way (like for the MIDACO algorithm), their sign must be changed before each call to the external algorithm solving routine.

#### 3.4. Intermediate printings

During the calculation phase, it is possible to print some intermediate results into the ProSimPlus history file (extension .HIS). These printings are performed through the use of a temporary file, named **IMPI\_OPTI.tmp** being located in the temporary folder of the current user. This file must be open at each call to the **OPTI** function and closed before leaving it so that the calling process can read its content and destroy it after.

If no information is required, it is not necessary to create this file. This can be the case if the external algorithm manages its own output files, nevertheless in such a case the content of these files could not be inserted neither in the simulation report nor in the history file.

#### 3.5. Graphical User Interface

The following screenshots present the modifications realized in the ProSimPlus "Optimization" unit in order to make possible the use on an external optimization algorithm.

The main tab, containing the parameters has been redesigned in order to clearly split the general parameters from the parameters relating to the "tear" streams (**Unfeasible Path** approach) from those relating to the selected optimization algorithm.

#### Selection of the optimization algorithm

🎝 Op	otimization (\$OPTI)					— 🗆	×
Name:	Optimization						
Desc:							
Identific	cation Parameters Scripts	Report Streams	Notes Advanced para	of the optimization	algorithm		
Optir	nizer properties		Tear streams		Algorithm		
	mber of periods mber of inequality constraints	1	□ 1 □ 2 □ 3 □ 4		Successive Quadratic Progra Successive Quadratic Progra External library the gradient		~
Nu	mber of rest steps	2	6		Kuhn Tucker parameter	0,0001	
	ximum number of runs in MCN	1000			Constraints violation	0,0001	
Ma	ximum number of iterations	200	All None	e	Non evolution of criterion	0,0001	
Pri	nting interval (iterations)	1	Iterative variables	Bounds and increments	Non evolution of variables	0,0001	
Actio	on variables Bounds and increments		Pressure	Bounds and increments Bounds and increments Bounds and increments	Scaling of the constraints		
					9	<u>D</u> K <u>C</u> ar	ncel

#### Other parameters of the "Optimization" unit

Optimization (\$OPTI)		– 🗆 X
Name: Optimization	Parameters relative to t	the selected algorithm
Desc:		
Identification Parameters Scripts Report Streams	s Notes Advanced parameters	
Optimizer properties	Tear streams	Algorithm
Number of periods     1       Number of inequality constraints     0       Number of rest steps     2       Maximum number of runs in the MCN     1000		Successive Quadratic Programming (SQP)         Successive Quadratic Programming (SQP)         External library         the gradient         Kuhn Tucker parameter         0,0001
Maximum number of iterations 200	All None	Non evolution of criterion 0,0001
Printing interval (iterations)	Iterative variables	Non evolution of variables 0,0001
Action variables	Temperature Bounds and increments      Pressure Bounds and increments	Scaling of the constraints
Bounds and increments	Partial flowrates Bounds and increments	<u>Q</u> K <u>C</u> ancel
General parameters and variables (bounds and in		variables,

#### Parameters relative to the external algorithm

Algorithm						
External	l library			ection field of the external		
Library:				libra	ary (DLL)	
Number	of parameters:	10			nber of parameters for the	
Index	Name	Parameter	^		ernal algorithm	
1		0				
2		0				
3		0				
4		0				
5		0		Parameters of the external algorithm: name, value		
6		0		algo	prithm: name, value	
7		0				
•			× -			

#### 3.6. Simulation report

The simulation report displays the generic elements of the "Optimization" unit, like the data relative to the objective function(s), to the constraints and to the optimization variables. It displays also the items relative to the standard numerical parameters of the unit: action variables and bounds, "tear" streams and bounds. Finally it displays the user-defined parameters as they are defined in the grid with their names and numerical values. If a printing subroutine is implemented the outputs made in this procedure are included at the end of the "standard" printings.

#### 4. USE CASE: THE MIDACO SOLVER

This section details a use case based on the implementation of an external algorithm. The solver selected has been developed by M. Schlueter and M. Munemoto from the Hokkaido University. It implements a general purpose algorithm for solving mono and multi-objective problems, initially developed for solving nonlinear problems with mixed variables (MINLP). In its current version, it is based on an evolutionary algorithm known as **« Ant Colony Optimization »**, from which it takes its name: **M**ixed Integer **D**istributed **Ant Colony Optimization**.

An evaluation version, limited to up to 4 optimization variables is available on the following web-site <u>www.midaco-solver.com</u>. It is the version which has been used in this example.

The problem used as a test case is a simple optimization problem for which the analytical solution is known as well as the solution provided by the ProSimPlus standard SQP algorithm.

It is a purely theoretical problem described as follows: a process has 4 feeds which are mixed and the aim is to maximize the following function which depends on the flowrates of these feeds.

$$f = -(f_1 + f_2 + f_3 + f_4)$$

With:

$$f_1 = \frac{1}{(x_1 - 1.111)^2 + 0.1}, \qquad f_2 = \frac{1}{(x_2 - 2.222)^2 + 0.1}$$
$$f_3 = \frac{1}{(x_3 - 3.333)^2 + 0.1}, \qquad f_4 = \frac{1}{(x_4 - 4.444)^2 + 0.1}$$

And

*x<sub>i</sub>* Total molar flowrate of the feed #i

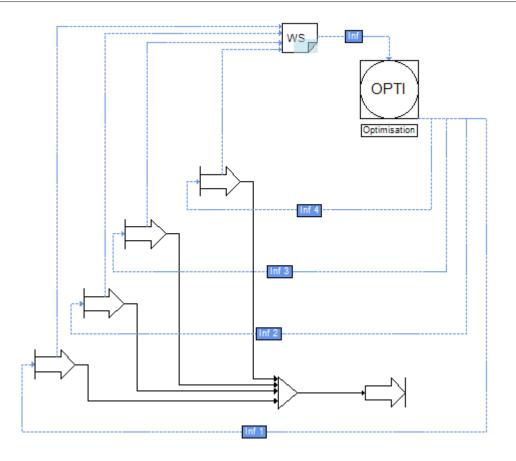
The analytical solution is:

$$f = -40$$

And  $x_1 = 1.111$ ,  $x_2 = 2.222$ 

$$x_3 = 3.333, \quad x_4 = 4.444$$

The objective function is calculated thanks to a script unit which takes the values of the feeds flowrates (inlet information streams) and the "Optimization" unit calculates them. It is a problem without constraints and the ProSimPlus flow diagram is presented hereafter:



The variables are bounded between 0.1 kmol/h and 10 kmol/h

The use of the ProSimPlus standard SQP algorithm with the default numerical parameters (except for the bounds) gives the following results:

SUCCESSIVE QUADRATIC PROGRAMMING ALGORITHM ************************************	
NUMBER OF VARIABLES OF THE PROBLEM AMONG WHICH Ø ARE TEAR STREAM VARIABLES AND 4 ARE OPTIMIZATION VARIABLES	4
NUMBER OF CONSTRAINTS OF THE PROBLEM	0
NUMBER OF EQUALITY CONSTRAINTS	0
NUMBER OF INEQUALITY CONSTRAINTS	0
DERIVATES OF THE FUNCTION ARE COMPUTED - BY 1ST ORDER FINITE DIFFERENCES NUMERICAL PARAMETERS:	
MAXIMUM NUMBER OF MAJOR ITERATIONS	200
MAXIMUM NUMBER OF SEQUENCE CALCULATIONS	
TOLERANCE ON KUHN-TUCKER ERROR	
TOLERANCE FOR NON-EVOLUTION OF THE FONCTION	
RESULTS:	
NUMBER OF ITERATIONS	
NUMBER OF RUNS IN THE PROCESS	130
- Inf	-39.9992

#### --> THE LAST ITERATION GIVES AN OPTIMAL SOLUTION

	VALUE	LOW. BOUND	UPP. BOUND	PERTURBATION	TYPE
OPTIMIZATION VARIABLES:					
1: Inf 1 2: Inf 2 3: Inf 3 4: Inf 4	1.110 2.221 3.331 4.442	0.1000 0.1000 0.1000 0.1000	10.00 10.00 10.00 10.00 10.00	1.0000E-03 1.0000E-03 1.0000E-03 1.0000E-03	PROPORTIONAL PROPORTIONAL PROPORTIONAL PROPORTIONAL

The source code of the procedure calling the MIDACO algorithm is provided in appendix 1.

The screenshot below shows the specific algorithm-parameters, the first 12 of them correspond to the **PARAM()** array of the MIDACO routine, the following ones are used to access to other parameters and are detailed in the MIDACO user's guide (MAXTIME, PRINTEVAL, SAVE2FILE and NI).

Externa	l library	~
Library:	MIDACO	Release\MIDACO.dl
Number	of parameters:	16
Index	Name	Parameter
1	ACCURACY	0
2	SEED	0
3	FSTOP	0
4	ALGOSTOP	0
5	EVALSTOP	100
6	FOCUS	0
7	ANTS	30
8	KERNEL	5
9	ORACLE	0
10	PARETOMAX	0
11	EPSILON	0
12	CHARACTER	0
13	MAXTIME	300
14	PRINTEVAL	1
15	SAVE2FILE	2
16	NI	0

In the studied example, the results obtained strongly depend on the values given to the parameters **ANTS** and **KERNEL** which with the default values (0 and 0) lead to a non-optimal solution.

With the above parameters, the results obtained are presented hereafter.

EXTERNAL OPTIMIZATION ALGORITHM \*\*\*\*\*\*

NUMBER OF VARIABLES OF THE PROBLEM AMONG WHICH Ø ARE TEAR STREAM VARIABLES AND 4 ARE OPTIMIZATION VARIABLES	4
NUMBER OF CONSTRAINTS OF THE PROBLEM NUMBER OF EQUALITY CONSTRAINTS NUMBER OF INEQUALITY CONSTRAINTS	0 0 0
PARAMETERS OF THE EXTERNAL ALGORITHM: ACCURACY	0 0 0 100.000 0 30.0000 5.00000 0 0 0 300.000 1.00000 2.00000 0
NUMERICAL PARAMETERS: MAXIMUM NUMBER OF MAJOR ITERATIONS MAXIMUM NUMBER OF SEQUENCE CALCULATIONS	
RESULTS: NUMBER OF ITERATIONS NUMBER OF RUNS IN THE PROCESS VALUE OF THE OBJECTIVE FUNCTION: - Inf	501

#### --> THE LAST ITERATION GIVES AN OPTIMAL SOLUTION

	VALUE	LOW. BOUND	UPP. BOUND	PERTURBATION	TYPE
OPTIMIZATION VARIABLES:					
1: Inf 1 2: Inf 2 3: Inf 3 4: Inf 4	1.114 2.218 3.329 4.441	0.1000 0.1000 0.1000 0.1000	10.00 10.00 10.00 10.00	1.0000E-03 1.0000E-03 1.0000E-03 1.0000E-03	PROPORTIONAL PROPORTIONAL PROPORTIONAL PROPORTIONAL

One can note that the parameters described in the graphical user interface are printed in the simulation report.

For this example, an additional printing routine is implemented, which transfers in the simulation report the content of the MIDACO\_SOLUTION.TXT file when the variable SAVE2FILE has a non-zero value. The source code of the printing routine is provided in appendix 2.

#### APPENDIX 1 - SOURCE CODE OF THE EXTERNAL **OPTI** ROUTINE

```
integer(4) function OPTI(PAR,NPT,ITEMAX,NAPM,IALP,ITER,KOPT,INFO, &
                     NCO,NCI,NVA,NF,F,C,X,XL,XU,AC,G,CN) result(rc)
!dec$ attributes stdcall, reference, alias:'OPTI', dllexport :: OPTI
   use IFWIN
   implicit none
                        :: NPT, ITEMAX, NAPM, IALP(NVA), NCO, NCI, NVA, NF
   integer(4), intent(in)
   integer(4), intent(inout) :: ITER, KOPT, INFO
              intent(inout) :: PAR(NPT)
   real(8),
                        :: F(NF), C(NCO), XL(NVA), XU(NVA), AC(NVA)
              intent(in)
   real(8),
   real(8),
              intent(inout) :: X(NVA), G(NF,NVA), CN(NCO,NVA)
   integer(4), parameter :: OPTI_CONVERGED = 0
   integer(4), parameter :: OPTI_FAILED
                                      = 2
   integer(4), parameter :: OPTI RUNNING
                                     = -1
   ! Dimensions of the optimization problem
   integer(4) O, N, NI, M, ME
   ! MIDACO information and stop flags
   integer(4) IFLAG, ISTOP
   ! MIDACO parameter
   real(8) PARAM(12)
   ! MIDACO integer 'IW' and real'RW' workspace and pareto front 'PF'
   integer(4), parameter :: LIW = 10000
   integer(4), parameter :: LRW = 10000
   integer(4), parameter :: LPF = 10000
   integer(4) IW(LIW)
   real(8) RW(LRW), PF(LPF)
   ! Parameter for stopping criteria, printing and license
   integer(4) MAXTIME, MAXEVAL, PRINTEVAL, SAVE2FILE, I
   character(len=60) :: KEY = 'MIDACO_LIMITED_VERSION___[CREATIVE_COMMONS_BY-NC-ND_LICENSE]'
   real(8), allocatable :: C1(:)
   integer(BOOL) rcDel
   logical Found
   integer(4) IOS, rcTemp, szTempPath
   character(len=256) TempPath
   if (KOPT /= 0) goto 100
   !CC Step 0: Deleting possible output files
                                           inquire(FILE='MIDACO_HISTORY.TXT', exist=Found)
   if (Found) rcDel = DeleteFile('MIDACO_HISTORY.TXT')
   inquire(FILE='MIDACO_SOLUTION.TXT', exist=Found)
   if (Found) rcDel = DeleteFile('MIDACO_SOLUTION.TXT')
   inquire(FILE='MIDACO_SCREEN.TXT', exist=Found)
   if (Found) rcDel = DeleteFile('MIDACO_SCREEN.TXT')
   inquire(FILE='MIDACO_PARETOFRONT.TXT', exist=Found)
   if (Found) rcDel = DeleteFile('MIDACO_PARETOFRONT.TXT')
   !CC Step 1: Problem definition
```

```
1
    Step 1.A : Problem dimensions
1
    1
O = NF
              ! Number of objectives
N = NVA
              ! Number of variables (in total)
NI = nint(PAR(16))
              ! Number of integer variables (0 <= NI <= N)</pre>
M = NCO
              ! Number of constraints (in total)
ME = NCO - NCI
              ! Number of equality constraints (0 <= ME <= M)
if (M /= 0) then
   if (allocated(C1)) deallocate(C1)
  allocate(C1(M))
else
   if (allocated(C1)) deallocate(C1)
   allocate(C1(1))
end if
C1(:) = 0.D0
!CC Step 2: Choose stopping criteria and printing options
                                             н
! Step 2.A : Stopping criteria
MAXEVAL = NAPM
                    ! Maximum evaluation budget (e.g. 1000000)
MAXTIME = nint(PAR(13))
                    ! Maximum time limit (e.g. 300 = 10 Min)
! Step 2.B : Printing options
PRINTEVAL = nint(PAR(14)) ! Print-Frequency for current best solution (e.g. 1000)
SAVE2FILE = nint(PAR(15)) ! Save SCREEN and SOLUTION to TXT-files [0=NO/1=YES]
!CC Step 3: Choose MIDACO parameters (FOR ADVANCED USERS)
                                             22222222222
1
!PARAM( 1) = 0.D0 ! ACCURACY
!PARAM( 2) = 0.D0 ! SEED
!PARAM( 3) = 0.D0 ! FSTOP
!PARAM(4) = 0.D0 ! ALGOSTOP
!PARAM( 5) = 0.D0 ! EVALSTOP
!PARAM( 6) = 0.D0 ! FOCUS
!PARAM( 7) = 0.D0 ! ANTS
!PARAM( 8) = 0.D0 ! KERNEL
!PARAM( 9) = 0.D0 ! ORACLE
!PARAM(10) = 0.D0 ! PARETOMAX
!PARAM(11) = 0.D0 ! EPSILON
!PARAM(12) = 0.D0 ! CHARACTER
do I=1,12
  PARAM(I) = PAR(I)
end do
ITER = -1
! Print MIDACO headline with basic information
call MIDACO PRINT(1,PRINTEVAL,SAVE2FILE,IFLAG,ISTOP,F,C1,X,XL, &
             XU,O,N,NI,M,ME,RW,PF,MAXEVAL,MAXTIME,PARAM,1,0,KEY)
KOPT = 15
I.
!
     Call MIDACO by Reverse Communication
```

```
I
   100 continue
   ! Incrementation of the iteration counter
   ITER = ITER + 1
   ! Sign change for the inequality constraints
   if (M /= 0) then
       C1(1:M) = C(1:M)
      do I=ME+1,M
         C1(I) = -C1(I)
       end do
   end if
   ! Opening the specific history file (if SAVE2FILE >= 2)
   if (SAVE2FILE >= 2) then
       szTempPath = len(TempPath)
      rcTemp = GetTempPath(szTempPath, TempPath)
       if (rcTemp > szTempPath .or. rcTemp == 0) then
          TempPath = '.\'
          rcTemp = 2
      end if
      open(UNIT=888,FILE=TempPath(1:rcTemp)//'IMPI_OPTI.tmp',STATUS='REPLACE',IOSTAT=IOS)
      write(888,1)
      1
                                                             ###',/, &
             '### SOLUTION FORMAT:
                                   F(1:0)
                                            G(1:M)
                                                     X(1:N)
             write(888,2) 0,M,N
2
       format('#',/, &
                                       N ',/, &
             '#
                     0
                              Μ
             '#',/, &
             3I10)
      call SAVE_HISTORY(1,0,N,M,F,C1,X,888,ISTOP)
      close(888)
   end if
   call MIDACO(1,0,N,NI,M,ME,X,F,C1,XL,XU,IFLAG, &
  &
              ISTOP, PARAM, RW, LRW, IW, LIW, PF, LPF, KEY)
   ! Call MIDACO printing routine
   call MIDACO_PRINT(2,PRINTEVAL,SAVE2FILE,IFLAG,ISTOP,F,C1,X, &
                   XL,XU,O,N,NI,M,ME,RW,PF,MAXEVAL,MAXTIME,PARAM,1,0,KEY)
   if (ISTOP == 0) then
      rc = OPTI_RUNNING
   else
      select case (IFLAG)
      case (1:7)
          rc = OPTI_CONVERGED
       case default
          rc = OPTI_FAILED
      end select
      select case (IFLAG)
       case (1, 3, 5, 7)
          INFO = 1
       case default
          INFO = IFLAG
      end select
      KOPT = 0
       if (allocated(C1)) deallocate(C1)
   end if
end function OPTI
```

#### APPENDIX 2 - SOURCE CODE OF THE EXTERNAL **IOPTI** ROUTINE

```
subroutine IOPTI(PAR,NPT)
!dec$ attributes stdcall, reference, alias:'IOPTI', dllexport :: IOPTI
    use IFWIN
    implicit none
    integer(4), intent(in) :: NPT
               intent(in) :: PAR(NPT)
    real(8),
    integer(4) IOS, rc, SAVE2FILE, szTempPath
    character(len=256) TempPath, LINE
    SAVE2FILE = nint(PAR(15))
    if (SAVE2FILE /= 0) then
        open(UNIT=889,FILE='MIDACO_SOLUTION.TXT',STATUS='OLD',IOSTAT=IOS)
        if (IOS /= 0) return
        szTempPath = len(TempPath)
        rc = GetTempPath(szTempPath, TempPath)
        if (rc > szTempPath .or. rc == 0) then
            TempPath = '. \'
            rc = 2
        end if
        open(UNIT=888,FILE=TempPath(1:rc)//'IMPO_OPTI.tmp',STATUS='REPLACE',IOSTAT=IOS)
        do while (.not.eof(889))
           read(889,'(A)') LINE
           write(888,'(A)') LINE
        end do
        close(888)
        close(889)
    end if
end subroutine IOPTI
```